

LIMITS , CONTINUITY AND GRAPH THEORY

1. $\lim_{x \rightarrow 1} \frac{x^3 - 2x^2 - x + 2}{(x^2 + x - 2)}$ is
a) 1 b. 2/3 c. - 2/3 d. 3/2

2. $\lim_{x \rightarrow 3} \left[\frac{1}{x-3} - \frac{3}{x(x^2 - 5x + 6)} \right]$ is
a. 0 b. 3/4 c. 4/3 d. - 4/3

3. $\lim_{x \rightarrow 0} \frac{1}{x} \sin^{-1} \left(\frac{2x}{1+x^2} \right)$ is
a. - 2 b. 2 c 0 d. ∞

4. $\lim_{x \rightarrow 0} \frac{1 - \cos 4x}{\cos 6x - \cos 4x} =$
a. 4/5 b. - 4/5 c. 1 d. 8/5

5. The least integer n for which

$\lim_{x \rightarrow 0} \frac{e^x - \sin x - \cos x}{x^n}$ is finite and non zero is

- a. 0 b. 1 c. 2 d. 3

6. $\lim_{\theta \rightarrow 0} \frac{\sin^2 \theta \cdot \tan 4\theta}{\tan 2\theta^2 \sin 3\theta}$ is
a. 2/3 b. 4/3 c. 3/4 d. 3/2

7. $\lim_{x \rightarrow 2} \frac{\sqrt{2x^2 - 1} - \sqrt{3x + 1}}{\sqrt{x^3 + 1} - \sqrt{2x + 5}}$ is

- a. $3/\sqrt{7}$ b. $2\sqrt{7}$ c. $3/2\sqrt{7}$ d. $3/4\sqrt{7}$

8. $\lim_{n \rightarrow 0^+} \frac{1^2 + 2^2 + 3^2 + \dots + n^2}{2n^3 + 3n^2 + 5}$ is

- a. $1/12$ b. $1/6$ c. $2/3$ d. $1/30$

9. $\lim_{n \rightarrow \infty} [(2^n + 1)(7^n + 10^n)]^{\frac{1}{n}}$

- a. $10/3$ b. 10 c. 20 d. 30

10. $\lim_{x \rightarrow \infty} \sqrt{x}(\sqrt{2x+1} - \sqrt{2x-1})$ is

- a. $2\sqrt{2}$ b. $\sqrt{2}$ c. $1/\sqrt{2}$ d. $-1/\sqrt{2}$

11. $\lim_{x \rightarrow \infty} \left(\frac{x+4}{x+2}\right)^x$ is

- a) e^2 b) e^6 c) e^3 d) 0

12. $\lim_{x \rightarrow 1} \left(\frac{1+x}{2+x}\right)^{\frac{1-\sqrt{x}}{1-x}}$ is

- a. $\sqrt{2/3}$ b. $2/3$ c. $4/9$ d. $8/27$

13. $\lim_{x \rightarrow 0^+} \frac{a^{\tan x} - a^{\sin x}}{\tan x - \sin x}$ is

- a. $\log a$ b. $-\log a$ c. $\tan x$ d. 1

14. The value of $f(0)$, so that the function $f(x) = \frac{2x - \sin^{-1}x}{2x + \tan^{-1}x}$ is continuous at each point in its domain, is
- a. $-1/3$ b. 0 c. $1/3$ d. 3

15. If function $f(x) = \begin{cases} \frac{1 - \cos 4x}{x^2} & \text{for } x < 0 \\ m & \text{for } x = 0 \\ \frac{\sqrt{x}}{\sqrt{16 + \sqrt{x-4}}} & \text{for } x > 0 \end{cases}$

- Is continuous at $x = 0$ then the value of m is
- a. 0 b. 2 c. 4 d. 8

16. if $f(x) = \begin{cases} \frac{|x|}{x} & x \neq 0 \\ 0 & x = 0 \end{cases}$

Then which of the following is true.

- a. Left hand limit = Right hand limit b. Limit does not exist
 c. $f(x)$ is continuous at $x = 0$ d. $f(x)$ is differentiable at $x = 0$

17. The function $f(x) = \begin{cases} 2x - 1 & \text{if } x < -1 \\ 3x^2 + 1 & \text{if } -1 \leq x < 3 \\ x^3 + 1 & \text{if } 3 \leq x < 4 \end{cases}$ Is discontinuous at
- a. -1 b. 3 c. -1, 3 d. none of these

18. If $f(x) = \begin{cases} \frac{x e^{\frac{1}{x}}}{1 + e^{\frac{1}{x}}} & x \neq 0 \\ \frac{k}{2} & x = 0 \end{cases}$

Is continuous at $x = 0$ then the value of k is

- a. -1 b. 2 c. 0 d. 1

19. Which of the following is true always

- a. If $f(x)$ is continuous at $x = a$ then it is differentiable at $x = a$
- b. If $f(x)$ and $g(x)$ are continuous at $x = a$
Then $(f(x) - g(x))$ need not be continuous at $x = a$
- c. Every polynomial function is continuous in the region $(-\infty, \infty)$
- d. None of these.

20. Let $f(x) = [x] + [-x]$ where $[]$ denotes greatest integer part then for any integer m

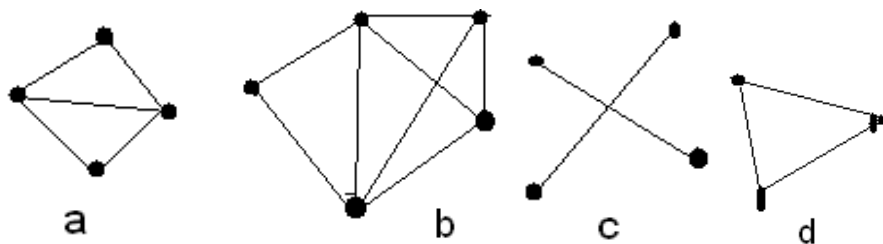
- a. $f(x)$ is continuous at $x = m$
- b. $\lim_{x \rightarrow m} f(x)$ exists but $\neq f(m)$
- c. $\lim_{x \rightarrow m} f(x)$ does not exist
- d. $f(x)$ is differentiable at $x = m$

21. If $f(x) = \begin{cases} \frac{\sqrt{1+mx} - \sqrt{1-mx}}{x}, & -1 < x < 0 \\ \frac{2x-1}{x-2}, & 0 < x \leq 1 \end{cases}$ is continuous in $[-1, 1]$

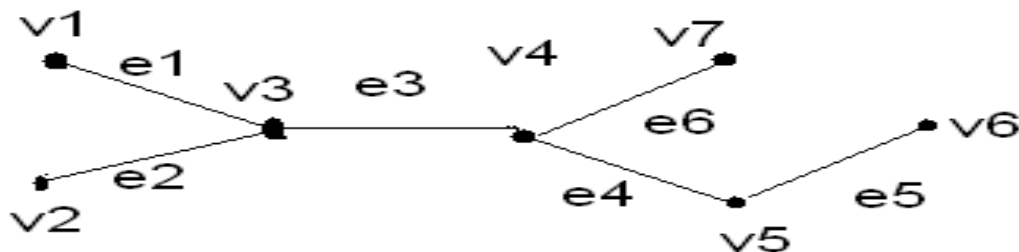
Then the value of m is

- a. 2 b. $\frac{1}{2}$ c. $-\frac{1}{2}$ d. -2

22. Which of the following is an Euler graph?

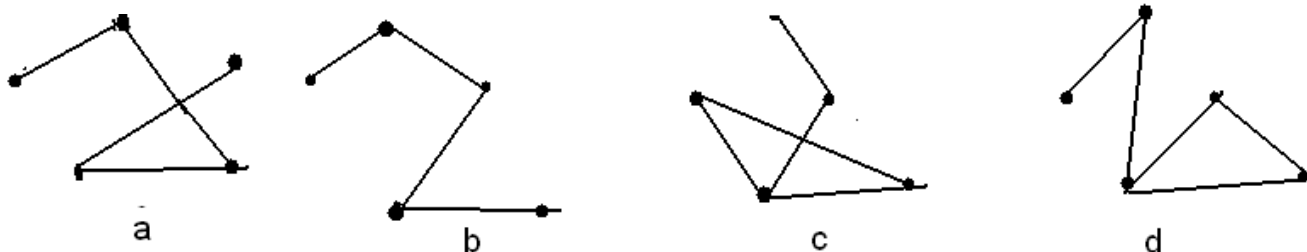
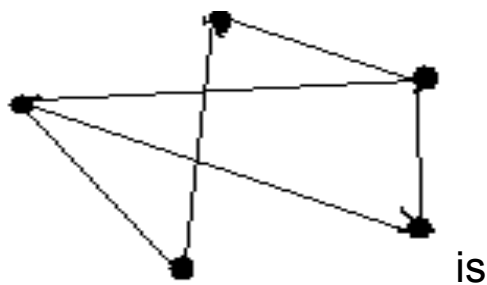


23. If m is the number of cut vertices and n is the number of bridges in a given graph then $m+n$ is

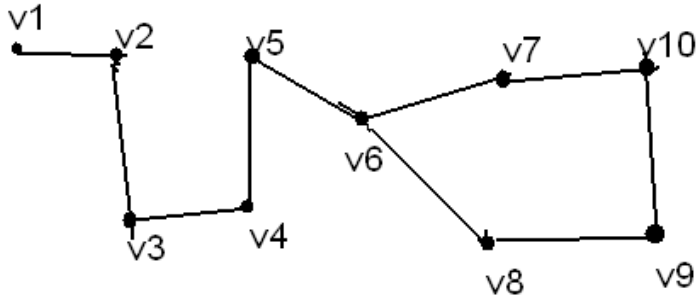


- a. 11 b. 6 c. 7 d. 9

24. The compliment of the given graph



25. The length of longest cycle and longest path for a given graph



- a) (5,10) b)(6,10) c) (5,9) d) (6,8)

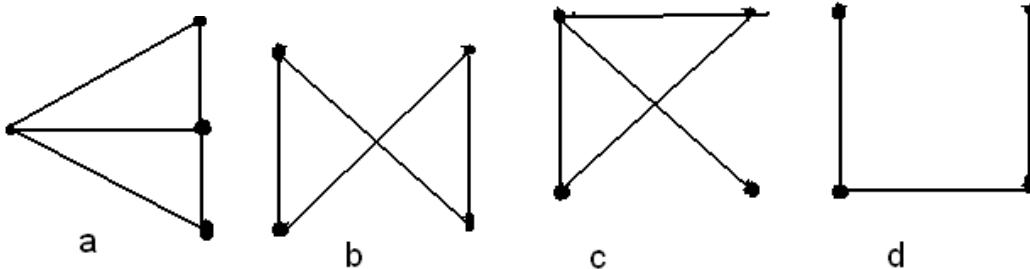
26. If sum of the degrees of all Vertices of a graph **G** is 24, then the number of edges in that graph is

- a. 23. b. 10 c. 6 d. 12

27. The number of edges in a complete graph of 'n' vertices is

- a. n b. n(n-1) c. $\frac{n(n-1)}{2}$ d. n/2

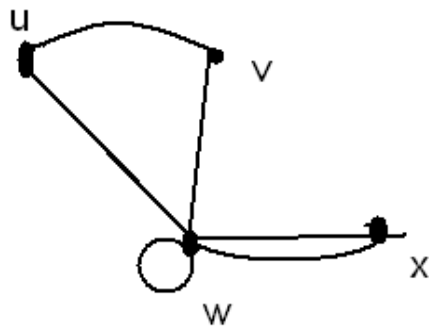
28. Which of the following is a bipartite graph ?



29. If F , V , E denote faces, vertices, and edges of polyhedron respectively then Euler's formula is

- a. $F+E = V+2$
- b. $F+V = E+2$
- c. $V+E = F+2$
- d. $F+V = 2E$

30.



In the above graph degree of w is

- a. 4
- b. 5
- c. 6
- d. 7

31. A graph is called pseudograph if

- a. It has no loops and no multiple edges.
- b. It has multiple edges and no loops.
- c. It has both multiple edges and loops.
- d. It is a tree.

32. An isolated vertex is

- a. Not a cut vertex.
- b. A cut vertex.
- c. A complete graph.
- d. Of degree one

33. If $f(a) = 3$, $g(a) = 2$, $f'(a) = 1$ and $g'(a) = -1$

Then $\lim_{x \rightarrow a} \frac{f(x)g(a) - f(a)g(x)}{x-a}$ is

- a. 0 b. 5 c. -5 d. 6

34. $\lim_{x > 1} \frac{\sum_{m=1}^{100} x^m - 1}{x-1}$ is

- a) 1050 b) 5050 c) 1010 d) 5010

35. $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\tan^3 x - 3 \tan x}{\cos(x + \frac{\pi}{6})}$ is

- a. 12 b) 24 c) -12 d) -24

36. $\lim_{x \rightarrow 1} \frac{x^{\frac{1}{2}} + x^{\frac{1}{4}} - 2}{x^3 - 1}$ is

- a. 7/36
b. + 1/36
c. - 1/12
d. 7/12

37. $\lim_{n \rightarrow \infty} \frac{2^{-n}(n^2+5n+6)}{(n+5)(2n-1)}$ is

- a. 0
- b. 1
- c. ∞
- d. - 2

38. $\lim_{\theta \rightarrow \frac{\pi}{4}} \frac{\sqrt{2} - \cos\theta - \sin\theta}{(4\theta - \pi)^2}$ is

- a. 1/32
- b. 1/16
- c. $\frac{\sqrt{2}}{16}$
- d. $\frac{\sqrt{2}}{32}$

39. $\lim_{x \rightarrow 0} \frac{e^x - e^{x \cos x}}{x + \sin x}$ is

- a. 0
- b. 1
- c. 2
- d. - 1

40. $\lim_{x \rightarrow 0} \left(\frac{1 - \tan x}{1 - \sin x} \right)^{\operatorname{cosec} x}$ is

- a. 0
- b. 1
- c. e
- d. 1/e

41. $\lim_{x \rightarrow 0^+} \frac{\sin \sqrt{x}}{\sqrt[4]{x}}$ is

- a. 1
- b. 0
- c. -1
- d. $-\frac{1}{4}$

42. $\lim_{n \rightarrow \infty} \frac{3(2)^{n+1} - 4(5)^{n+1}}{5(2)^n + 8(5)^n}$ is

- a. $-\frac{5}{2}$
- b. $\frac{5}{2}$
- c. 10
- d. $-\frac{1}{4}$

43. $\lim_{x \rightarrow 0} \frac{(5)^x - (5)^{-x} - 2}{(x)^2}$ is

- a. $2 \log 5$
- b. $(\log 5)^2$
- c. 0
- d. 1

44. $\lim_{n \rightarrow \infty} \left[\frac{1}{1-n^2} + \frac{2}{1-n^2} + \frac{3}{1-n^2} + \dots + \frac{n}{1-n^2} \right]$ is

- a)0 b)4 c)1/2 d)-1/2

45. $\lim_{x \rightarrow 0} \frac{2^x + 3^x - 5^x - 7^x}{\tan x}$ is

- a) $\log_e 6/5$ b) $\log_e 6/35$ c) $\log_e 5/6$ d) $\log_e 6/15$

46. $\lim_{x \rightarrow \infty} \frac{(x)^n}{(e)^x}$ for all $n \in \mathbb{N}$ is

- a. e
- b. n!
- c. 0
- d. 1/e

47. $\lim_{x \rightarrow \infty} \left(\frac{x+5}{x+2} \right)^{2x+1}$ is

- a. e^4
- b. e^{-4}
- c. e^6
- d. e^2

48. $\lim_{\theta \rightarrow \frac{\pi}{6}} \frac{2 \sin^2 \theta + \sin \theta - 1}{2 \sin^2 \theta - 3 \sin \theta + 1}$ is

- a)0 b)-1 c)1 d)-3

49. $\lim_{x \rightarrow 1} \left(\frac{3}{1-x^3} - \frac{5}{1-x^5} \right)$ is

- a)0 b)1 c)-1 d)3

50. $\lim_{x \rightarrow \infty} \frac{(2x+3)^{40} (4x-1)^{10}}{(2x-5)^{50}}$ is
 a) 1 b) 2^{10} c) 2^5 d) 2^2

51. $\lim_{n \rightarrow \infty} \left(\frac{1+3+5+\dots +n \text{ terms}}{2+4+6+\dots +n \text{ terms}} \right)^n$ is
 a) 1 b) 2 c) $1/e$ d) e

52. $\lim_{x \rightarrow 0} \frac{\tan^3 \sqrt[3]{x} \cdot \log(1+3x)}{(\tan^{-1} \sqrt{x})^2 (e^{\sqrt[3]{x}} - 1)}$ is
 a. $\frac{1}{2}$ b. 3 c. 0 d. $\frac{1}{3}$

53. $\lim_{\theta \rightarrow 0} \frac{\sin \theta^2 (1 - \cos \theta^2)}{\theta^6}$ is
 a. $\frac{1}{2}$ b. $\frac{1}{4}$ c. 0 d. $\frac{1}{3}$

54. $\lim_{x \rightarrow \frac{\pi}{4}} \frac{1 - \cot x}{2 - \operatorname{cosec}^2 x}$ is
 a. $-\frac{1}{2}$ b. 1 c. $\frac{1}{4}$ d. $\frac{1}{2}$

55. If $f(x) = \begin{cases} \frac{x^2 - c^2 x + 2c}{2x^2 - 5x + 2} & x \neq 2 \\ 1 & x = 2 \end{cases}$
 Is continuous at $x = 2$ then the value of c
 a. ± 1 b. 1 c. -1 d. 0

56. The function $f(x) = [x] + |1 - x|$ where $[x]$ greatest integer x is
- Continuous at $x = 1$
 - Dis continuous at $x = 1$
 - Limit as $x \rightarrow 1$ does not exist
 - Derivable at $x = 1$

57. If $f(x) = \begin{cases} \frac{\sin 3x}{x^3 + 4x} & x \neq 0 \\ \frac{k}{2} & x = 0 \end{cases}$

Is continuous at $x = 0$ then value of k is

- $\frac{3}{4}$
- $\frac{4}{3}$
- $\frac{3}{2}$
- $\frac{2}{3}$

58. Which of the following is false statement

- If $f(x)$ is continuous at $x = a$ then $\lim_{x \rightarrow a} f(x)$ exists.
- If $f'(a)$ exists then $f(x)$ is continuous at $x = a$
- If $f(x)$ is continuous at $x = a$ the $f'(a)$ exists
- If $\lim_{x \rightarrow a} f(x) = f(a)$ $f(x)$ is continuous at $x = a$

59. The function $f(x) = \frac{1 - \sin x + \cos x}{1 + \sin x + \cos x}$ is not defined at $x = \Pi$ The value of $f(\Pi)$

so that $f(x)$ is continuous at $x = \Pi$ is

- $-\frac{1}{2}$
- $\frac{1}{2}$
- 1
- 1

60. If $f(x) = \begin{cases} \frac{\sin(e^{x-2} - 1)}{\log(x-1)} & \text{when } x \neq 2 \end{cases}$ is continuous at $x=2$ then $f(2)$ is

- e
- e^2
- e
- 1

61. If $f(x) = \begin{cases} \frac{\log_e(1+2x) - \log_e(1-2x)}{x} & \text{if } x \neq 0 \\ e^n & \text{if } x = 0 \end{cases}$

is continuous at $x=0$. then the value of n is

- a) 4 b) e^4 c) $\log_e 4$ d) $\log_4 e$

62. If $f(x) = \begin{cases} \frac{\sin[x]}{[x]} & [x] \neq 0 \\ 0 & [x] = 0 \end{cases}$

where $[]$ denotes greatest integer part

$\lim_{x \rightarrow 0} f(x)$ is equal to

- a) 1 b) -1 c) 0 d) none of these

63. Which of the following is a False statement?

- a) In a graph, every edge of a tree is a bridge .
- b) In a graph Edge set E can be an empty set .
- c) Every graph must have even number of vertices of odd degree.
- d) In any tree there must be at least one pendent vertex.

64. In a complete K_n regular graph the degree of each vertex is

- a) $n(n-1)/2$ b) $n/2$ c) $n-1$ d) n

65. The number of edges and vertices of K_5 graph is

- a) 15, 5
- b) 15, 4
- c) 10, 4
- d) 10, 5

66. The point of discontinuity of the function

$$f(x) = \lim_{n \rightarrow \infty} \left(\frac{4^n (\sin^2 x)^n}{3^n - (4 \cos^2 x)^n} \right) \text{ is}$$

- a) $n\pi \pm \frac{\pi}{3}$ b) $n\pi \pm \frac{\pi}{6}$ c) $n\pi \pm \frac{5\pi}{6}$ d) $n\pi \pm \frac{2\pi}{3}$

$$67. \lim_{x \rightarrow 0} \left[\frac{|\sin x| + |\sin^2 x| + |\sin^3 x| + \dots + \infty}{x} \right] \text{ is}$$

- a)1 b)0 c)2 d)-1

$$68. \lim_{x \rightarrow 0} \frac{x \tan 2x - 2x \tan x}{(1 - \cos 2x)^2} \text{ is}$$

- a)2 b)-2 c)1/2 -d)-1/2

$$69. \lim_{x \rightarrow 0} \left[\frac{e^{\frac{1}{x}} - 1}{(1 + e^{\frac{1}{x}})} \right] \text{ is}$$

- a) 1 b)0 c)does no exists d)none of these

$$70. \lim_{n \rightarrow \infty} \left[1 - \frac{2}{3} + \frac{4}{9} - \frac{8}{27} + \dots n \text{ terms} \right] \text{ is}$$

- a)2/3 b)3/5 c)-3/5 d)5/3